

# Broadband, few-cycle mid-infrared continuum based on the intra-pulse difference frequency generation with BGSe crystals

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**Abstract:** We demonstrate for the first time the generation of octave-spanning mid-infrared using a BGSe nonlinear crystal. A Cr:ZnS laser system delivering 28-fs pulses at a central wavelength of 2.4  $\mu\text{m}$  is used as the pump source, which drives the intra-pulse difference frequency generation inside the BGSe crystal. As a result, a coherent broadband mid-infrared continuum spanning from 6 to 18  $\mu\text{m}$  has been obtained. It shows that the BGSe crystal is a promising material for broadband, few-cycle mid-infrared generation via frequency down conversion with femtosecond pump sources.

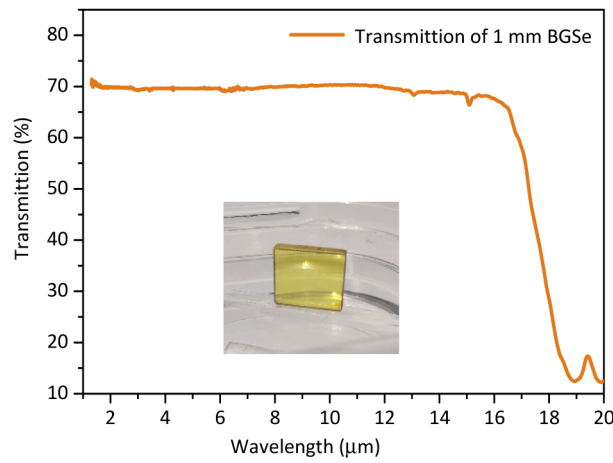
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## 1. Introduction

Mid-infrared (MIR) light in the range of 2–20  $\mu\text{m}$  is useful for chemical and biological identification due to the presence of many molecular characteristic absorption lines in this spectral region [1]. A coherent, few-cycle source with a simultaneous coverage of the broad MIR range can further enable new applications such as micro-spectroscopy [2,3], femtosecond pump-probe spectroscopy [4], and high-dynamic-range sensitive measurements [5–7]. Until now numerous schemes have been developed to generate coherent MIR radiation, such as synchrotron beam lines, quantum cascade lasers, supercontinuum sources [2], optical parametric oscillators (OPO) [8] and optical parametric amplifiers (OPA). These schemes all have their own strengths and weaknesses in terms of complexity, bandwidth, power, efficiency, and pulse durations. Among them, intra-pulse difference frequency generation (IDFG) is attracting growing attention thanks to the development of high-power femtosecond 2  $\mu\text{m}$  lasers that can effectively pump small-bandgap non-oxide nonlinear crystals to generate high-power broadband coherent MIR light [9–13]. Compared to the normally used OPOs and OPAs, IDFG allows a reduction in system complexity and enhancement of reliability, as the need to align two separate beams or cavities at high precision is removed. Besides, the MIR output is intrinsically carrier-envelope-phase (CEP) stable with IDFG [7].

For the purpose of broadband coherent MIR generation with IDFG, suitable nonlinear media with a wide transparency range, large nonlinear coefficient and high damage threshold are called for. A number of nonlinear crystals have been successfully utilized to generate coherent broadband MIR by IDFG, including LiGaS<sub>2</sub> (LGS) [14], GaSe [9–13,15], ZGP [11,16], and ZnSe/ZnS [17]. The parameters of these MIR sources are summarized in Table 1. Yet the exploration of new nonlinear crystals for MIR generation is far from complete. In 2010, a new biaxial chalcogenide

nonlinear crystal, BaGa<sub>4</sub>Se<sub>7</sub> (BGSe), has been fabricated using the Bridgman-Stockbarger method [18,19]. It has a wide transparency range from 0.47 to 18  $\mu\text{m}$  (as shown in Fig. 1) with nonlinear coefficients of  $d_{11} = 24.3$  pm/V and  $d_{13} = 20.4$  pm/V. The transparency window of BGSe is significantly broader than ZGP and LGS although its nonlinearity is lower than ZGP ( $75 \pm 8$  pm/V) [20]. In contrast to GaSe, BGSe can also be cut at the desired phase-matching angle and can be anti-reflection coated. Recently another new chalcogenide nonlinear crystal BGGSe was developed and used for MIR generation [21,22], showing very similar transparency window and higher nonlinear coefficient ( $d_{11} = 66$  pm/V) compared to BGSe. However, BGSe crystal can be more easily grown to a large dimensions to accommodate larger beam sizes [19]. These make BGSe a promising nonlinear crystal for high power, broadband MIR generation.



**Fig. 1.** Transmission spectrum of the 1-mm-thick uncoated BGSe crystal. The inset shows the actual crystal used in this experiment.

**Table 1. Summary of the parameters with selected IDFG sources. *NL crystal*, nonlinear crystal;  $\lambda_{\text{pump}}$ , pump wavelength;  $\tau$ , pulse duration of the pump pulses;  $f_{\text{rep}}$ , repetition rate of the pump pulses;  $P_{\text{pump}}$ , pump average power;  $P_{\text{MIR}}$ , average power of the MIR generated by IDFG;  $\lambda_{\text{MIR}}$ , spectral span of MIR;  $\eta$ , conversion efficiency.**

<i>NL crystal</i>	$\lambda_{\text{pump}}$ [ $\mu\text{m}$ ]	$\tau$ [fs]	$f_{\text{rep}}$ [MHz]	$P_{\text{pump}}$ [W]	$P_{\text{MIR}}$ [mW]	$\lambda_{\text{MIR}}$ [ $\mu\text{m}$ ]	$\eta$ [%]	<i>Ref.</i>
LGS	1.03	19	100	50	103	6.8-16.4	0.21	[14]
ZnSe	2.09	15	77	7	25	2.7-20	0.36	[17]
ZnS	2.09	15	77	7	35	2.7-15	0.5	[17]
GaSe	2.09	15	77	7	24	4.4-20	0.34	[9]
GaSe	1.95	16	1.25	32	450	6-18	1.41	[12]
GaSe	2.5	20	78	6	13	4.3-16.6	0.22	[11]
ZGP	2.5	20	78	4.5	148	5.8-12.5	3.3	[11]
GaSe	2.4	28	69	3.4	15	2.7-17	0.44	[10]
BGSe	2.4	28	69	1.1	1.9	6-18	0.17	[this work]

Efficient MIR generation has been reported with BGSe crystals in the schemes of OPA, OPO and difference-frequency mixing [23–31]. In all these works, pulses longer than a picosecond were used as the driving sources for the parametric conversion, and a simultaneous coverage of the broad MIR range has not been realized with BGSe crystals. In this work, we demonstrate the generation of a coherent MIR output with a BGSe crystal via IDFG. Driven by femtosecond

pulses at 2.4  $\mu\text{m}$ , the resulting spectrum simultaneously covers the range between 6 and 18  $\mu\text{m}$ . This is, to the best of our knowledge, the broadest MIR spectrum generated from frequency down conversion using a BGSe crystal to date. The damage threshold of the BGSe crystal was also characterized under femtosecond pulses with a central wavelength of 2.4  $\mu\text{m}$ .

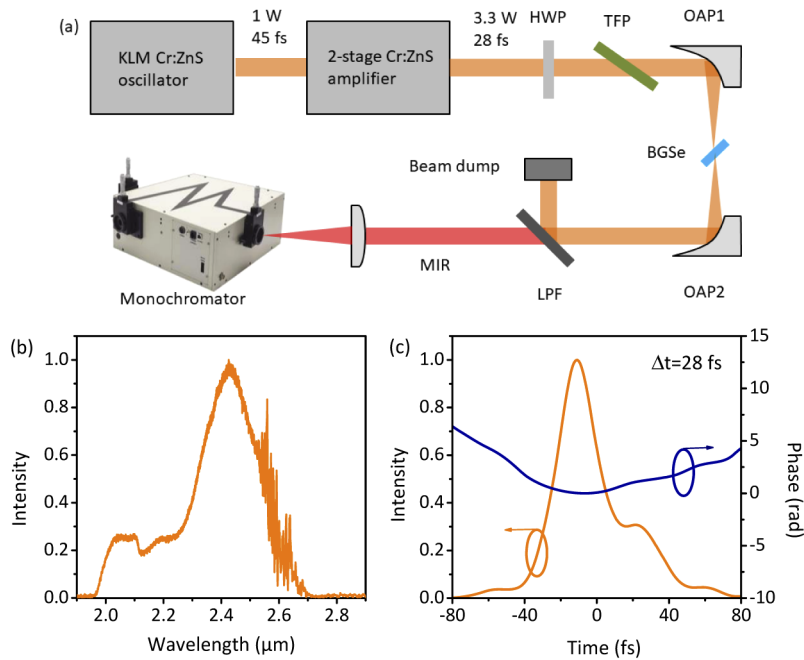
## 2. Experimental setup

The experimental setup is illustrated in Fig. 2(a). The driving pulses are initially generated from a home-built Kerr-lens mode-locked Cr:ZnS oscillator [32–36] with a polycrystalline Cr:ZnS crystal ( $5 \times 2 \times 9 \text{ mm}^3$ , transmission=15% at 1908nm) as the gain medium pumped by a Tm-doped fiber laser at 1908nm. The oscillation in a standing-wave cavity delivers 45-fs pulses operating at a repetition rate of 69 MHz with an average power of 1 W at a carrier wavelength of 2.4  $\mu\text{m}$ . The power is amplified to 3.3 W in a home-built two-stage single-pass polycrystalline Cr:ZnS amplifier ( $5 \times 2 \times 6 \text{ mm}^3$ , transmission=20% at 1908nm and  $5 \times 2 \times 9 \text{ mm}^3$ , transmission=15% at 1908nm) [10], and the output pulse duration is measured with a home-built second-harmonic-generation frequency-resolved optical grating (SHG-FROG) apparatus. The retrieved pulse duration, at 28 fs (Fig. 2(c)), corresponds to 3.5 optical cycles of the carrier wave at 2.4  $\mu\text{m}$ . Figure 2(b) shows the spectrum after the amplification stage spanning from 2 to 2.6  $\mu\text{m}$ , which determines the interacting wavelength range through the IDFG process. Compared to pumping at 1  $\mu\text{m}$ , the use of longer pump wavelengths enables the use of highly nonlinear non-oxide crystals with broad mid-IR transparency to achieve the desired broadband phase matching. In addition, a lower photon energy can mitigate multiphoton absorption in the nonlinear crystal, enabling a higher damage threshold of the crystal. Furthermore, the conversion efficiency of IDFG can also be enhanced, as it scales quadratically with the effective interaction length, which lengthens as the pump wavelength increases [11].

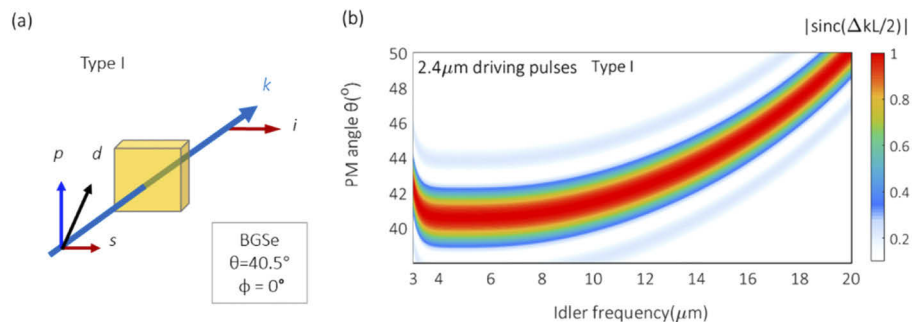
The driving pulses were focused by a gold-coated off-axis parabolic mirror into a 1-mm-thick, uncoated BGSe crystal (DIEN TECH) down to a spot diameter of 46  $\mu\text{m}$ . The BGSe crystal is cut at an angle of  $\theta=40.5^\circ$  and  $\varphi=0^\circ$  for Type I phase matching, as shown in Fig. 3(a). We optimized the phase matching condition by rotating the crystal and a half-wave plate. The generated MIR radiation was separated from the transmitted fundamental driving beam by long-pass filters and then sent to a power meter and a monochromator (Newport Cornerstone 260) for power and spectral measurement, respectively.

The driving power was set as 1.1 W to keep it below the damage threshold. The corresponding peak intensity in the focus was 37.3  $\text{GW}/\text{cm}^2$  taking into account the high reflection loss of the uncoated BGSe. The generated MIR was focused by a ZnSe lens into the monochromator for the spectral measurement. To suppress second-order diffractions from the monochromator's grating, three long-pass filters with cut-on wavelengths at 4.5, 7.3, and 11  $\mu\text{m}$  were used, and three different spectra spanning from 4.5 to 8.5  $\mu\text{m}$ , 6 to 13  $\mu\text{m}$ , and 10 to 22  $\mu\text{m}$  were recorded, respectively. A silicon nitride infrared emitter (Bentham Instruments Ltd) was used to calibrate the intensities of the measured spectra and correct for losses in the long-pass filters and the ZnSe lens, and the low diffraction efficiency of the monochromator grating at longer wavelengths (starting from 11  $\mu\text{m}$ ). The corrected spectra were then stitched together to obtain the final spectrum.

The measured spectrum shown in Fig. 4(a) covers the wavelength range from 6 to 18  $\mu\text{m}$  (at  $-30 \text{ dB}$ ), which can support few-cycle pulses in the MIR. We simulated the spectrum numerically based on the one-dimensional (1D) + time split-step method [37], where spatial effects such as walk-off and self-focusing were not considered. With the measured FROG data of the driving pulses as the input, the output IDFG spectrum was simulated, as shown in Fig. 4(a). The simulated spectrum matches well with the experimental result in the wavelength range of 6-18  $\mu\text{m}$ . The dip in the wavelength around 15  $\mu\text{m}$  in the experimental spectrum results from the absorption lines of carbon dioxide in the beam path to the monochromator, which was not considered in the

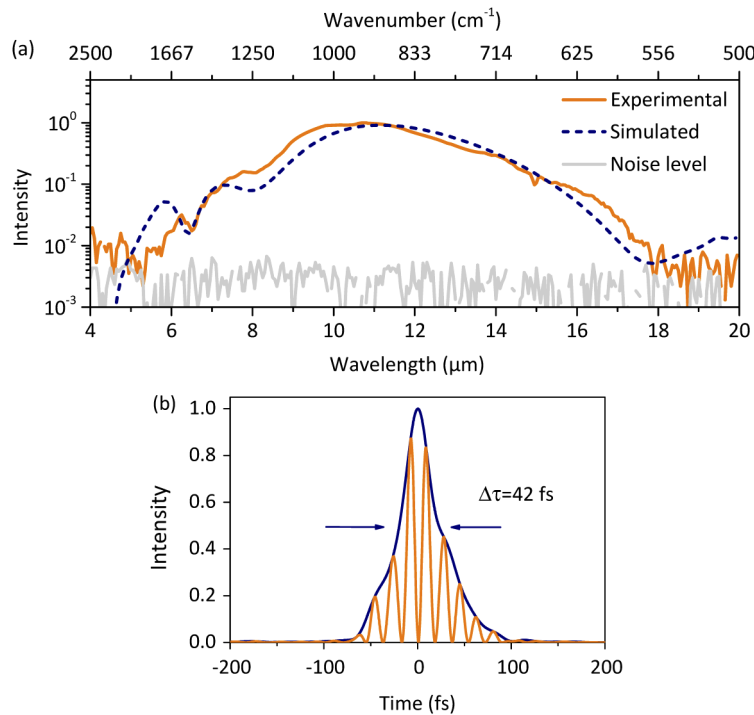


**Fig. 2.** (a) Experimental setup of the MIR generation with a BGSe crystal. OAP, off-axis parabolic mirror with an effective focus length of 20 mm; HWP, half-wave plate; TFP, thin-film polarizer; LPF, long-pass filter. (b) Measured spectrum of the driving pulses. (c) Corresponding temporal profile retrieved from a SHG-FROG measurement, showing a pulse duration of 28 fs.



**Fig. 3.** (a) Type I phase-matching scheme in biaxial BGSe crystals. The arrows indicate polarizations ( $d$ : driver;  $p$ : pump;  $s$ : signal;  $i$ : idler) and wave vector ( $k$ ). (b) Optimal phase matching angle and phase matching function  $|\text{sinc}(\Delta kL/2)|$  in a BGSe crystal with respect to the generated signal (idler) with a 2.4  $\mu\text{m}$  pump beam.

simulation. Figure 4(b) shows the numerically simulated temporal characteristics of the MIR pulses, and the predicted pulse duration, directly after the crystal, of 42 fs—corresponding to almost one optical cycle for pulses at the carrier wavelength of 11  $\mu\text{m}$ . The Fourier transform limit is even shorter at 29 fs for the simulated spectrum and 22 fs for the experimentally measured spectrum. A pulse duration of less than one optical cycle at the wavelength of 11  $\mu\text{m}$  could therefore be expected if the dispersion of the BGSe crystal and the long-pass filter in the MIR beam path, which amounts to  $\sim 1500 \text{ fs}^2$ , can be compensated.



**Fig. 4.** (a) The experimentally measured and numerically simulated MIR spectrum. (b) Simulated pulse shape (black curve) and absolute electrical field intensity (red curve) of the MIR pulses.

An average power of 1.2 mW was measured (S302C, Thorlabs) behind the long-pass filter with a cut-on wavelength of 4.5  $\mu\text{m}$ . Taking into account the  $>10\%$  loss of the long-pass filter above 4.5  $\mu\text{m}$  and the reflection loss due to the uncoated BGSe crystal surface, the generated MIR power inside the crystal can be calculated as 1.9 mW, which can already fulfill many applications in field-resolved detection. Further investigation on power scaling, such as by increasing the focus spot size while keeping the intensity the same, could potentially yield even higher output power.

With a band gap of 2.64 eV, BGSe crystal has been reported to have a damage threshold of  $100 \text{ MW/cm}^2$  at 1.064  $\mu\text{m}$  and  $122.2 \text{ MW/cm}^2$  at 2.1  $\mu\text{m}$ , respectively [25,26]. Both values were obtained with nanosecond pulses as the pump. Here the damage threshold is specified with femtosecond pulses at 2.4  $\mu\text{m}$  by increasing the average power of the driving pulses until damage was observed, characterized by a sudden drop in transmitted power and the appearance of a visible damage hole on the front surface and cracks on the crystal. Two crystals were tested and both exhibited damage at 1.3 W, which corresponds to a peak intensity of approximately  $40.5 \text{ GW/cm}^2$ . The damage threshold is currently limited by the crystal quality, which can be improved further in the future according to the manufacturer.

### 3. Conclusion

In conclusion, we have demonstrated a MIR source with the BGSe crystal based on the IDFG method. A femtosecond Cr:ZnS laser system at the wavelength of 2.4  $\mu\text{m}$  was used as the driving source, enabling a simultaneous spectral coverage from 6 to 18  $\mu\text{m}$ . To the best of our knowledge, this is the first time broadband MIR generation has been realized in a BGSe crystal. The output is expected to have few-cycle pulse durations and also to be stable in its carrier-envelope phase. Compared to other crystals in Table 1, the preliminary result with BGSe shows a MIR generation with comparable broad bandwidth (wider than ZGP and LGS) although with a lower average power and conversion efficiency. Higher average power could be expected with further optimization of the focus spot size and crystal thickness. A better crystal quality with higher damage threshold would also be beneficial for increasing the MIR average power and conversion efficiency. This work shows that BGSe crystal is a promising material for the broadband, coherent MIR generation.

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### Disclosures

The authors declare no conflicts of interest.

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